

Distinguishing Dark Energy from Modified Gravity

- Define an effective energy-momentum tensor of missing matter:

$$T_{\text{eff dark}}^{\mu\nu} \equiv \frac{1}{8\pi G} G^{\mu\nu} - \sum_{\text{known } a} T_a^{\mu\nu}$$

If the visible sectors satisfy the equivalence principle then necessarily

$$\left(T_{\text{eff dark}}^{\mu\nu} \right)_{;\nu} = 0$$

SB, arXiv:0707.0692;

Hu & Sawicki, arXiv:0708.1190

Then any visible dynamics can be “explained” by effective dark dynamics that is assumed to affect the visible species by Einstein equations.

Linearly:

Kunz & Sapone, astro-ph/0612452;

Zukin & Bertschinger, arXiv:0801.2431

Most generally:

SB, arXiv:0707.0692;

Hu & Sawicki, arXiv:0708.1190

- Nevertheless, modified gravity can be detected, in view of its **conceptual distinctions** from GR:

1. Some dark species may couple non-covariantly to the metric $g_{\mu\nu}$, which controls the dynamics of the visible species.

2. The gravitational action may be not $S_{\text{grav}} = \frac{1}{16\pi G} \int d^4x \sqrt{-g} R$

Detecting Modified Gravity

- If gravity is not governed by general relativity then:
 1. The inferred effective dark dynamics is expected to violate the equivalence principle. Then we could observe that
 - a. The inferred laws for local dark dynamics depend on the distribution of visible matter SB, arXiv:0707.0692;
Hu & Sawicki, arXiv:0708.1190

(This dependence should be more drastic than what could be explained by possible non-gravitational coupling between dark and visible matter.)
 - b. The inferred dark dynamics is **superluminal**

(Yet note that superluminality is physically admissible and may coexist with regular general relativity, e.g.,
[Babichev, Mukhanov, Vikman 07](#))
 2. Propagation of **gravitational waves** may deviate from predictions of the Einstein equations Kahya and Woodard 07

(Of course, there are complimentary, non-cosmological, tests for general relativity: Hulse-Taylor pulsar, frame-dragging, etc.)